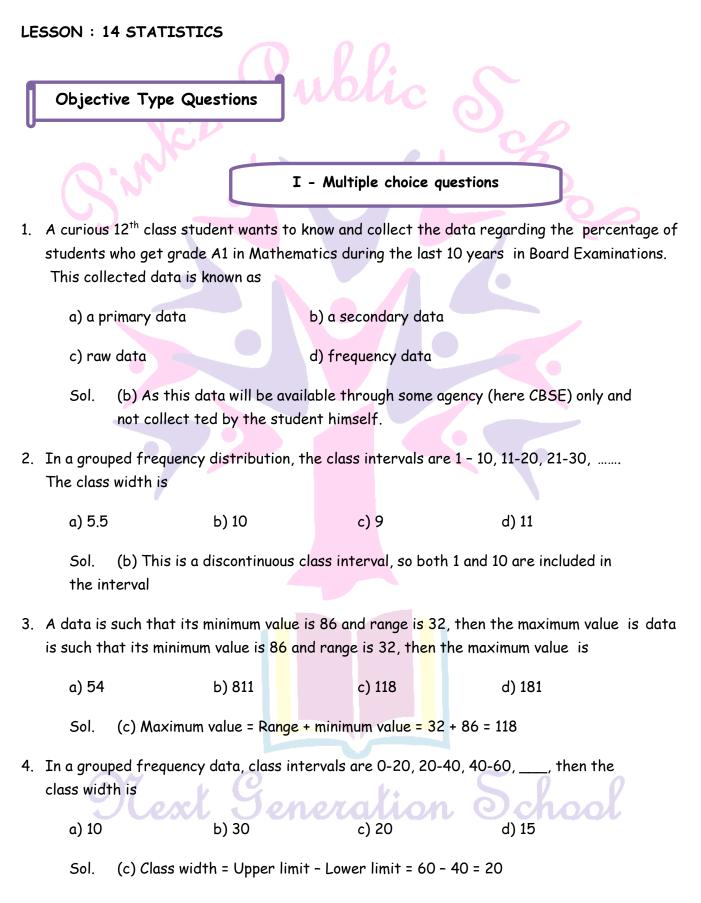
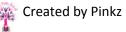


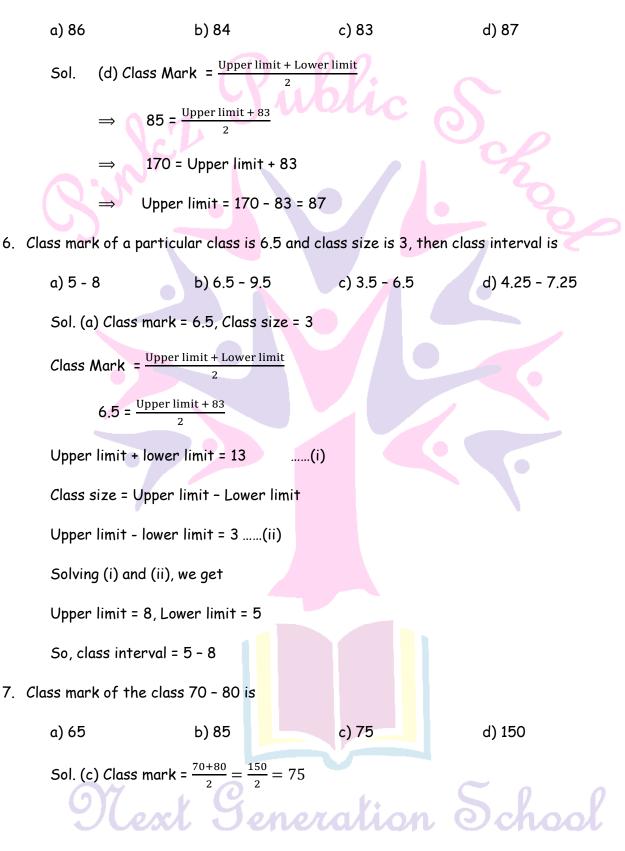
GRADE -9







In continuous frequency distribution, class mark of a class is 85 and lower limit is
 83, then its upper limit is





8. In a frequency distribution, the mid-value of a class is 10 and the width of the class is
6, The lower limit of the class is

a) 6 b) 7 c) 8 d) 12 Sol. (b) Mid - value = 10 So, Upper limit = Lower limit = 2 (mid-value) Upper limit = Lower limit = 2 × 10 = 20(i) Upper limit - Lower limit = Class width ∴ Upper limit - Lower limit = 6(ii) Solving (i) and (ii) we get ∴ Upper limit = 13, Lower limit = 7

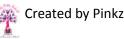
9. Which is more reliable: primary data or secondary data and why?

Sol. Primary data is more reliable and relevant because the investigator himself collected the data according to his plan and objective in view.

10. Why do we group data?

- Sol. If the number of observations in the data is large and the difference between maximum and minimum value of observation is more, then we condenses the data into station of data in a more meaningful way.
- 11. Which table gives a better picture of data: frequency distribution table for ungrouped data or frequency distribution table for grouped data?
 - Sol. Frequency distribution table for grouped data.
- 12. State any two characteristics of statistics.
 - Sol. (i) The data for statistics should be collected with a definite purpose in view
 - (ii) Statistics in an experiment should be comparable.
- 13. Find the upper limit of the first class interval of the following
 - 8 11, 12 15, 16 19, [CBSE 2015]

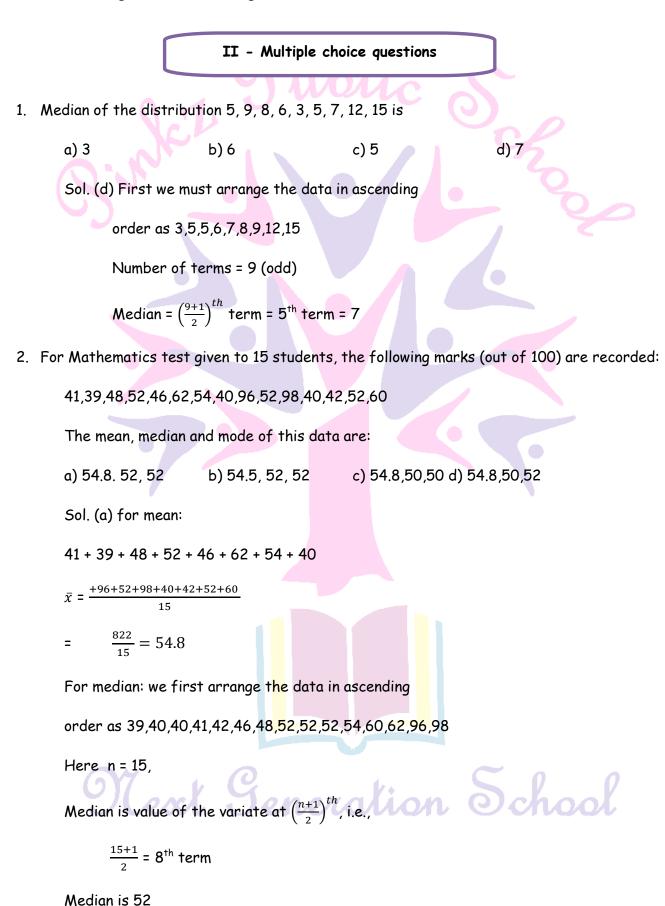
Sol. Upper limit of 8 - 11, is 11





14. Find the range of the given data 25.7, 16.3, 2.8, b21.7, 24.3, 22.7 and 24.9

Sol. Range of the data = Highest value - Lowest value = 25.7 - 2.8 = 22.9



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For mode: we notice from above arrangement 52 occurs maximum number of times Hence Mode = 52 .

- 3. Mean of 20 observations is 15.5. litre, it was found that the observation 24 was misread as 42. The corrected mean is :
 - a) 14.2 b) 14.8 c) 14.0 d) 14.6
 - Sol. (d) sum of 20 observations = 20 x 15.5 = 310

Corrected sum = 310 - 42 + 24 = 292

- Corrected mean = $\frac{292}{20}$ = 14.6
- 4. Given below are the seats won by different political parties in the polling outcome of state assembly election:

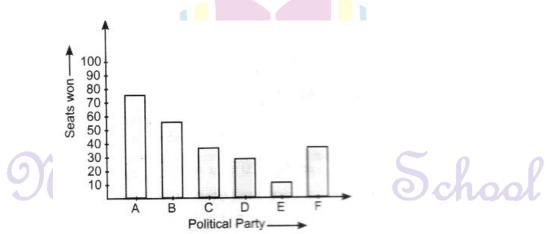
Political Party	A	В	С	D	E	F	
Seats won	75	55	37	29	10	37	

The graphical representation will be

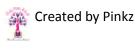
- a) a histogram
- b) a vertical bar graph or a horizontal bar graph
- c) a frequency polygon curve

d) none of these

Sol. (b) Vertical bar graph representing the polling results of a state assembly election.



This can also be represented by a horizontal bar graph.





- 5. In histogram also we use bars and values. How it is different from bar graph?
 - a) No difference
 - b) Histograms are same as bars but joined together
 - c) we use 3 class intervals instead of variables.
 - Sol. (c) In Histogram, we use class intervals instead of variables.
- 6. A frequency polygon can be
 - a) drawn using variables
 - b) drawn using bar graph
 - c) drawn independently and by using histogram
 - Sol. (c)
- 7. Mode of the data , 4,6,9,6,4,2,4,8,6,4,3,4,6 is
 - a) 6 b) 4 c) 3

Sol. (b) 4occuring five times [maximum times]

8. One day, I decided to sit in a shoe shop and observe, I noticed that out of shoes numbers 6,7,8, or 9, there were maximum sale from shoe number 8. Which measure of central tendency gives the average?

d) 2

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a) me	an	b) median		c) mode		
Sol. (c) mode					
9. If the m	ean of the obs	ervations				
<i>x</i> , <i>x</i> +	3, <i>x</i> + 5, <i>x</i> + 7	, <i>x</i> + 10				
is 9,	the mean of th	ne last three ob	servations i	S		
a) 10	<u>1</u> 3	b) $10\frac{2}{3}$		c) $11\frac{1}{3}$	~	d) $11\frac{2}{3}$
Sol. (c) Mean = <u>x,+ x</u> -	+3+x+5+x+7+x 5	+ 10	ion	Sch	vool
\Rightarrow	9 = $\frac{5x+25}{5} \Rightarrow \frac{5x+25}{5}$	45 = 5x + 25				
⇒	$5x = 20 \Rightarrow x$	c = 4				



- \therefore Last these observations are
- 4 + 5, 4 + 7, 4 + 10, i.e., 9,11,14
- :. Mean = $\frac{9+11+14}{3} = \frac{34}{3} = 11\frac{1}{3}$
- 10. If \bar{x} represents the mean of a observations

 $x_{1}, x_{2}, \dots, x_{n} \text{ then value of } \sum_{i=1}^{n} (x_{i} - \bar{x}) \text{ [NCERT Examplar]}$ a) -1 b) 0 c) 1 d) n-1 Sol. (b) we have of $\sum_{i=1}^{n} (x_{i} - \bar{x}) = \sum_{i=1}^{n} x_{i} - \sum_{i=1}^{n} \bar{x}$ $= n(\bar{x}) - n(\bar{x}) = 0$ Where $\sum_{i=1}^{n} x_{i} = n\bar{x}$

and

 $\sum_{i=1}^{n} \bar{x} = n \bar{x}$

11. If each observation of the data is increased by 5. Then their mean []

[NCERT Exemplar]

- a) remains the same (b) becomes 5 times the original mean
- c) is decreased by 5

d) is increased by 5

Sol. (d) Let number of observations are n.

So $\sum_{i=1}^{n} x_i$ represents sum of observations

Each observation is increased by 5

So, sum of new (n + 5) observations is

- $= |\sum_{i=1}^{n} x_i| + n(5) n\bar{x} + n5 n(\bar{x} + 5)$
- \therefore Mean is increased by 5
- 12. The mid-value of a class interval is 42. If the class-size is 10. Find the upper and lower limits of the class [HOTS]

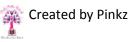
Sol. Mid-value of class interval is known s close-mark.

Given class - mark - 42 and class size = 10

So Lower class limit - Class mark - $\frac{1}{2}$ x Class size

$$= 42 - \frac{1}{2} \times 10 = 37$$

7



5 chool



Upper class limit = Class mark + - $\frac{1}{2}$ × Class size

$$= 42 + -\frac{1}{2} \times 10 = 47$$

13. The mean of x_1 and x_2 is 7 and mean of x_1, x_2, x_3 is 6, Find the value of x_3

Sol. We know that

Mean = $\frac{Sum of all observations}{Total number of observations}$ Now $7 = \frac{x_1 + x_2}{2} \Rightarrow x_1 + x_2 = 14$ (i) Also, $6 = \frac{x_1 + x_2 + x_3}{3}$ $\Rightarrow \qquad 6 = \frac{14 + x_3}{3}$ [:: From (i) $x_1 + x_2 = 14$] $\Rightarrow \qquad 14 + x_3 = 18$ $\Rightarrow \qquad x_3 = 18 - 14 = 4$

14. Find the mean of the factors of 24

[CBSE 2012]

Sol. Various factors of 24 = 1,2,3,4,6,8,12 and 24

Mean
$$\bar{x} = \frac{Sum \ of \ all \ observations}{Total \ number \ of \ observations}$$
$$= \frac{1+2+3+4+5+6+8+12+24}{8}$$
$$= \frac{60}{8} - \frac{15}{2} = 7.5$$

15. Find the mean of first six odd numbers

[CBSE 2016]

Sol. First six odd numbers are 1,3,5,7,9, and 11

: Mean
$$(\bar{x}) = \frac{1+3+5+7+9+}{6}$$

= $\frac{36}{6} = 6$

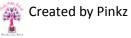
16. Find the mean of prime numbers between 30 and 40.

Sol. Prime numbers between 30 and 40 are 31 and 37 (only two)

11

: Mean
$$(\bar{x}) = \frac{31+37}{2}$$

= $\frac{68}{2} = 34$





17. The mean of the set of numbers 6,3,x, 4,3,5 and y is given as 5. What is the value of x + y? [CBSE 2016]

Sol. Total number of observations - 7

Mean of the data

$$\bar{x} = \frac{x_1 + x_2 + x_3 + x_4 + x_5 + x_6 + x_7}{7}$$

$$\Rightarrow 5 = \frac{6 + 3 + x + 4 + 3 + 5 y}{7}$$

$$\Rightarrow 21 + x + y = 35$$

$$\Rightarrow x + y = 35 - 21 = 14$$

18. Calculate the median of the given data 144, 145, 147, 148, 149, 150, 152, 155, 160

[CBSE 2015]

Sol. Here, number of observations (n) = 9 (odd)

$$\therefore \text{ Median} = \left(\frac{n+1}{2}\right)^{th} \text{ term}$$
$$= \left(\frac{9+1}{2}\right)^{th} \text{ observation}$$
$$= 5^{th} \text{ observation} = 149$$

19. If the median of the observations: x, x + 3, x + 5, x + 7, x + 10, is 9 find the last observation.

Sol. Total number of observations.

n = 5 (an odd number)

$$\therefore \text{ Median} = \left(\frac{n+1}{2}\right)^{th} \text{ observation}$$

$$\Rightarrow \qquad 9 = 3^{rd} \text{ observation} = x + 5$$

$$\Rightarrow \qquad x = 9 - 5 = 4$$
So the last observation = x + 10 = 4 + 10 = 14



20. The age (in years) of 12 persons are given below; 42,48,48,50,56,43,47,56,60,65,56,65 Find the mode. [CBSE 2016]

Sol. On arranging the data in ascending order. We get

42,43,47,48,48,50,56,56,56,60,65,65

Age 56 years occurs 3 times in the data and has maximum frequency amongs other.

- : Mode of age = 56 years
- 21. Find the mode of the following data

15,14,19,20,14,15,16,14,15,18,14,19,15,17,15

Sol. Making a frequency table, we have

<i>x</i> ₁	14	15	16	17	18	19	20	
f_1	4	5	1	1	1	2	1	

We find that observation 15 has the maximum frequency (5)

∴ Mode = 15

I – Short answer type questions

1. The marks obtained by 20 students of class IX in an examination are given below:

18,8,12,6,9,16,13,5,16,1<mark>5</mark>,<mark>3,</mark>1,13

Present the data in the form of a frequency distribution table using the equal class interval, one such class being 15 - 20 [CBSE 2014]

Sol. Required frequency distribution table is shown below:

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Mark obtained by students	Tally Marks	Frequency (Number of Students)	
0 - 5	winc	2	
5 - 10		6	
10 - 15	₩.	5	
15 - 20	Ш	4	
20 - 25	Ш	3	
Total		30	

2. The weights [in kilograms] of 25 students are given as follows:

35,38,36,<mark>37,38,35,37,36,35,36,36,37,</mark>37,<mark>35,38,36,35,36,37,37,38,36,38,37</mark>

Complete the following frequency table:

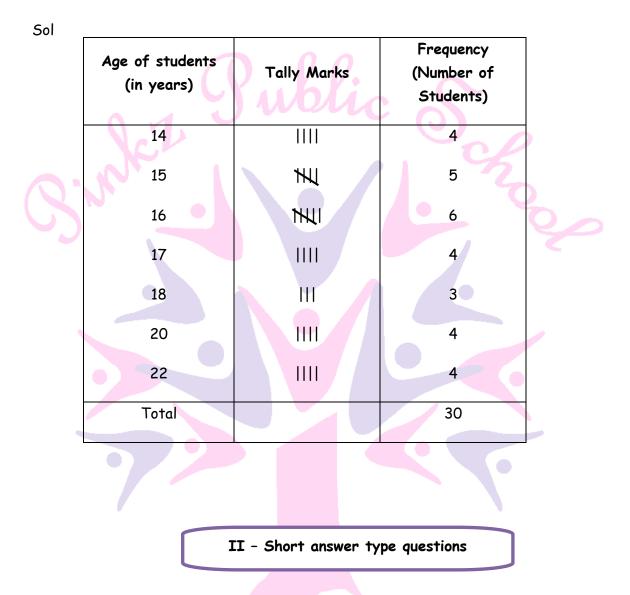
8
-
-

Sol.

				1	1	
	Weights (in Kg)	35	36	37	38	
	Frequency	5	7	7	6	
97	ext	Gen	erali	ion	Sch	ool



3. Given below the ages (in years) of 30 students of a class VIII th in a school, Prepare a discrete frequency distribution table.



1. The class marks of the distribution are 37,42,47,52, and 57. Determine the class-size and the class limits of the last class mark. [CBSE 2013]

Sol. Class size = Difference between class marks of two adjacent classes

= 42 - 37 - 5

Therefore, we need classes of size 5 with class marks as 37,42,47,52,57

Now lower class limit of the last class

ssation School $= 57 - \frac{1}{2} \times 5$ = 57 - 2.5 - 54.5



Upper class limit of the last class = 57 - $\frac{1}{2} \times 5$ = 59.5

 \therefore Class limits of the last class mark are 54.5 – 59.5

2. The mean of the observations x, 2x + 1, 2x + 5 and 2x + 9 is 30. What is the mean of first three observations?

Sol : Mean
$$\bar{x} = \frac{x + (2x+1) + (2x+5) + (2x+9)}{4} = 30$$

 $\therefore \quad 7x + 15 = 120$

$$\Rightarrow 7x = 120 - 15 = 105$$
$$\Rightarrow x = \frac{105}{7} = 15$$

So the first three observations are 15, 31 and 35.

Therefore their mean = $\frac{15+31+35}{3} = \frac{81}{3} = 27$

3. Find the mean of the first 8 prime numbers [CBSE 2015]

Sol. First eight prime numbers are 2,3,5,7,11,13,17 and 19

$$\therefore \text{ mean} = \frac{2+3+5+7+11+13}{17+19}$$

 $=\frac{77}{8}=9.625$

4. The following observations have been arranged in ascending order. If the median of the data is 23.5, find the value of x

12,16,17,19,*x*, *x* + 3, 27,37,38,40 [CBSE 2012]

Sol. Here number of observations (n) = 10 (even)

 $\therefore \text{ Median} = \frac{1}{2} \left[\left(\frac{n}{2} \right)^{th} \text{ term } + \left(\frac{n}{2} + 1 \right)^{th} \text{ term} \right]$ $= \frac{1}{2} \left[5th \text{ term } + 6th \text{ term} \right]$ $23.5 = \frac{1}{2} \left[x + x + 3 \right]$ $\Rightarrow 2x + 3 = 47$ $\Rightarrow 2x = 47 - 3 = 44$

$$\Rightarrow$$
 x = 22





5. Find the mode of the following marks (out of 10) obtained by 23 students

10,4,6,5,9,3,2,10,7,6,5,4,9,10,10,3,4,10,6,9

Sol. Arranging the data in ascending order, we have 2,3,3,4,4,4,5,5,6,6,6,7,9,9,9,10,10,10,10,10

Here the observation 10 has the maximum frequency 5

- : Mode = 10
- 6. For what value of 'x' the mode of the following data is 7?

3,5,6,7,5,4,7,5,6, (x+1),8,7 [[CBSE 2013]

Sol. Arranging the data in ascending order, we have 3,4,5,5,5,6,6,7,7,7,(x+1),8

Since mode of the given data is 7, so it should have the maximum frequency it means

 $x + 1 = 7 \Rightarrow x = 6$

III - Short answer type questions

 Make a frequency distribution table of the following marks scored by 20 students of a class, where class intervals are 4-7, 8-11 and so on: 5,11,6,8,10,20,23,14,19,22,7,11, 19,9,12,26,24,14,7,8

л.	Marks scored	Tally Marks	Frequency (Number of Students)
	4 - 7	1111	4
	8 - 11	1 11	7
	12 - 15		3
9	16 - 19 20 - 23	nertilio	n School
	24 - 27	II	2
	Total		20
		14	Created by Pinkz

10



2. The electricity bill (in rupees) of 25 hours in a locality are given below construct a frequency distribution table with a class size of 75.

170,212,252,225,310,712,415,430,320,328,194,197,235,318,412,535,604,726, 375,410,318, 405, 469,373,414.

Sol. The minimum and maximum value on the data is 170 and 726.

∴ Range - 726 - 170 - 556

Class size = 75

: Number of classes - $\frac{556}{752} = 7.4 \sim 8$

The classes, therefore, are 150 -225, 225-300, 300-375 and so on.

We therefore, construct the frequency distribution table as follows.

Electricity Bill (in Rupees)	Tally Marks	Frequency
150 - 225	1111	4
225 - 300	III	3
300 - 375	***	6
375 - 450	14411	7
450 - 525		1
525 - 600		1
600 - 675	I I	1
675 - 750	П	2
Total		25
Tart G	anaralia	n Sch



3. The marks obtained by 40 students of class IX in a mathematics test are given below

18,55,68,79,85,43,29,68,54,73,47,35,72,64,95,44,50,77,64,35,79,52,45,54,70,83, 62, 64,72,92,84,76,63,43,54,38,73,68,52,54.

Sol. The minimum and maximum marks in the given data are 18 and 95.

: Range = 95 - 18 = 77

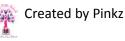
It is given that class size is 10. So

Number of classes =
$$\frac{Range}{Class size} = \frac{77}{10} = 7.7 = 8$$

So, we should have 7 classes each of size 10. According to minimum and miximum value. The classes should be 18-28, 28-38, 38-48 and so on. We, therefore, construct the frequency distribution table as follows.

Marks obtained	Tally Marks	Frequency [Number of Students]
18 - 28		4
28 - 38	11	3
38 - 48	##	6
48 - 58	1+4111	7
58 - 68	#41	1
68 - 78	7444_7744	1
78 - 88	ШИ	1
88 - 98	II	2
Total		25

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IV - Short answer type questions

1. Mean of 50 observations was found to be 80.4 But later on, it ws discovered that 96 was misread as 69 at one place. Find the correct mean. If in each observation a constant value 'k' is added, how is the mean affected? [CBSE 2012]

Sol. Given Mean of 50 obsrvations = 80.4

 $\therefore \text{Sum of 50 observations} = 50 \times 80.4 = 4020$

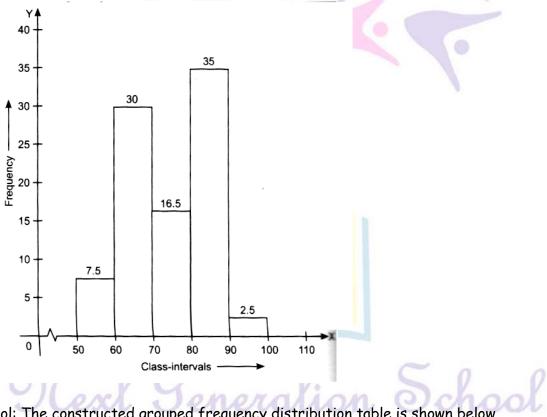
But later, it was discovered that 96 was misread as 69 at one place

: Correct mean = $\frac{4020-69+96}{50} = \frac{4047}{50} = 80.94$

Hence the correct mean = 80.94

* If 'k' is added to each observation, then new mean is 80.94 + k

2. Using the given histogram, prepare a grouped frequency distribution table [CBSE 2014]



Sol: The constructed grouped frequency distribution table is shown below



	Class interval	Frequency	
	50 - 60	7.5	
	60 - 70	0. 30	
0 v	70 - 80 80 - 90	16.5	
. Se	90 - 100	35	h
N'		2.5	00

3. The marks of 15 students in an examination out of 10 marks is as follows

3,9,7,5,6,3,7,6,7,4,7,7,4,8,2 Find the mean, mode and median. Sol. Arranging the given data in ascending order, we have

2,3,3,4,4,5,6,6,7,7,7,7,7,8,9,

Therefore

(i) Mean $\overline{x} = \frac{1}{N} \sum x_1 = \frac{1}{15} [\text{sum of all observations}]$

$$=\frac{1}{15} \times 86 = 5.67$$

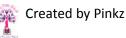
(ii) Here, the observation 7 has maximum frequency 5.

(iii) Here, number of observations (n) = 15 (odd)

$$\therefore \text{ Median} = \left(\frac{n+1}{2}\right)^{th} \text{ observation}$$

= 8th observation = 6







4. Draw a histogram for the following marks obtained [out of 100 marks] by class of 80 students [CBSE 2016]

	Marks	Number of Students	
	10 - 20	18	
	20 - 30	10	
	30 - 50	15	
5	50 - 60	7	
	60 - 80	4	

Sol. We observed that the class size are varying in frequency distribution table with minimum class size = 20 - 10 = 10 By using formula

Adjusted frequency of a class = $\frac{Minimum \ class \ size}{Class \ size \ of \ this \ class} \times frequency$

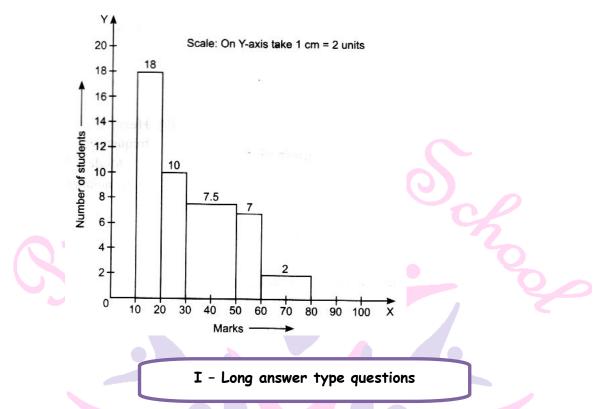
Accordingly the modified frequency distribution table is given below

Marks	Number of s (frequen		Width	Length of the rectangle (Adjusted frequency)
10 - 20	18		10	
20 - 30	10		10	$\frac{10}{10} \times 18 = 18$
30 - 50	15		20	$\frac{10}{10} \times 10 = 10$
50 - 60	7		10	$\frac{10}{20} \times 15 = 7.5$
60 - 80	4		20	$\frac{10}{10} \times 7 = 7$
N	ext G	ener	alio	$\sum_{20}^{10} \times 4 = 2$

Therefore, histogram ,for the above table is shown below:





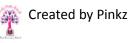


 Below are the marks obtained by 30 students of a class in maths test out of 100. Make a frequency distribution table for this data with class interval of size 10 and histogram to represent the dat.

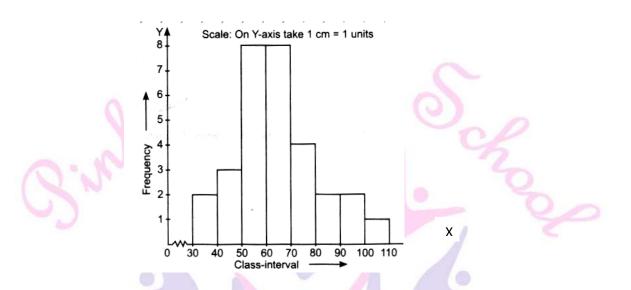
55,61, 46, 100, 75, 90, 77, 60,48, 58, 64, 59, 60, 78, 55, 88, 60, 78, 55, 88, 60, 37, 58, 84, 62, 44, 52, 50, 56, 98, 67, 70, 69, 68

Sol. Marks obtained by 30 students are 55,61, 46, 100, 75, 90, 77, 60,48, 58, 64, 59, 60, 78, 55, 88, 60, 78, 55, 88, 60, 37, 58, 84, 62, 44, 52, 50, 56, 98, 67, 70, 69, 68

Class Interval	Tally Marks	Frequency
30 - 40		2
40 - 50		3
50 - 60		8
60 - 70		8
70 - 80	INI	4
80 - 90	II	2
90 - 100		2 0
100 - 100	eneration	r Ochoo
Total		30

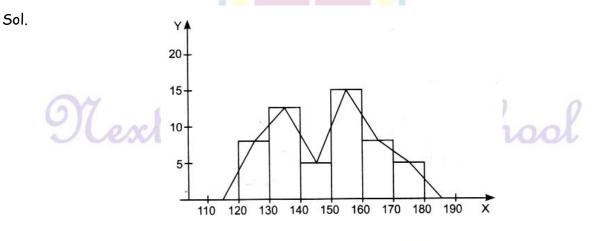






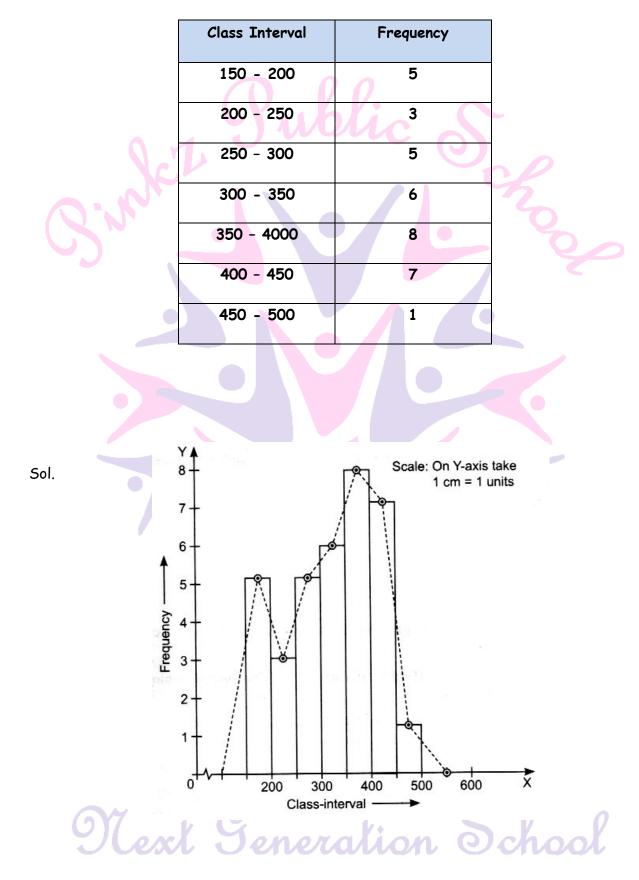
2. In a city, the following weekly instructions are made in a study on cost of living index. Draw a histogram and frequency polygon for the data.

Cost of living index	Number of weeks
120 - 130	8
130 - 140	12
140 - 150	4
150 - 160	16
160 - 170	8
170 - 180	4

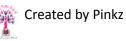


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3. Draw a histogram and frequency polygon on the same graph for the following data





4. Following are the runs scored by two teams A and B in a 10 over match. Represent the data graphically on the same graph.

	Overs	Team A	Team B	
	1	2	5	
	2	Manc	6	
	3	8	2	
S.3	4	9	10	
	5	4	5 6	
	6	5	6	
	7	6	3	
	8	10	4	
	9	4	8	
	10	2	10	



