Name :
Grade : VIII
Subject : Mathematics

## Chapter: 5. Data Handling

1. The height of rectangle in a fistogram shows the
[ $N$ (CERT Exemplar]
(a) Width of the class
(6) Upper limit of the class
(c) Lower limit of the class
(d) Frequency of the class
2. Ageometric representation showing the relationship between a whole and its parts is $a$ :
[ $N$ (CERT Exemplar]
(a) Pie chart
(6) Histogram
(c) Bar graph
(d) Pictograpf
3. In a pie chart, the total angle of the centre of the circle is:
[ $N$ (CERT Exemplar]
(a) $180^{\circ}$
(6) $360^{\circ}$
(c) $270^{\circ}$
(d) $90^{\circ}$
4. The range of the data $30,61,55,56,60,20,26,28,56$ is:
[ $N$ (CERT Exemplar]
(a) 26
(b) 30
(c) 41
(d) 61
5. Which of the following is not a random experiment?
[ $N$ (CERT Exemplar]
(a) Tossing a coin
(b) Rolling a dice
(c) Choosing a card from a deck of 52 cards
(d) Ifrowing a stone from a roof of a building
6. What is the probability of choosing a vowelfrom the alphabets?
[ $N$ (CERT Exemplar]
(a) $\frac{21}{26}$
(b) $\frac{5}{26}$
(c) $\frac{1}{26}$
(d) $\frac{2}{36}$
7. In a school only, 3 out of 5 students can participate in a competition. What is the probability of the students who do not make it to the competition?
[ $N$ (CERI Exemplar]
(a) 0.65
(6) 0.4
(c) 0.45
(d) 0.6

Students of a class voted for the ir favourite colour and a pie chart was prepared based on the data collected.

Observe the pie chart given below and answer questions $8-10$ based on it.

8. Which colour received $\frac{1}{5}$ of the votes?
[NCERI Exemplar]
(a) $\operatorname{Red}$
(6) Blue
(c) Green
(d) Yellow
9. If 400 students voted in all, then how many did vote 'Others' colour as the ir favour ite ?
(a) 6
(b) 20
(c) 24
(d) 40
10. Which of the following a reasonable conclusion for the given data?
[NCERI Exemplar]
(a) $\frac{1}{20}$ th student voted for 6 lue colour
(6) Green is the popular colour
(c) The number of students who voted for red colour is two times the number of students who voted for yellow colour
(d) Number of students liking together yellow and green colour is approximately the same as those for red colour.
11. Listed below are the temperature in ${ }^{\circ} \mathrm{C}$ for 10 days.-6,-8,-7, 0, 3, 2, 1, 5, 4, 4
[ $N$ (CERT Exemplar]
What is the range of the data?
(a) 8
(b) $13{ }^{\circ} \mathrm{C}$
(c) $10^{\circ} \mathrm{C}$
(d) $12^{\circ} \mathrm{C}$
12. Ram puts some buttons on the table. There were 46 lue, 7 red, 3 6lack and 6 white buttons in all. All of a sudden, a cat jumped on the table and knocked out one button on the floor. What is the probability that the button on the floor is blue?
[ $N$ (CERI Exemplar]
(a) $\frac{7}{20}$
(6) $\frac{3}{5}$
(c) $\frac{1}{5}$
(d) $\frac{1}{4}$
13. Raful, Varun and Yash are playing a game of spinning a coloured wheel. Raful wins, if spinner Cands on red. Varun wins, if spinner lands on 6 lue and Yasf wins, if it lands on green. Which of the following spinner should be used to make the game fair?
[NCERT Exemplar]

(iii)

(iv)
(a) (i)
(6) (ii)
(c) (iii)
(d) (iv)
14. In a frequency distribution with classes 0-10, 10-20 etc, the size of the class intervals is 10. The lower limit of fourth class is: [NCEERT Exemplar]
(a) 40
(6) 50
(c) 20
(d) 30
15. $\mathcal{A}$ coin is tossed 200 times and head appeared 120 times. Probability of getting a head in this experiment is
[NCERT Exemplar]
(a) $\frac{2}{5}$
(6) $\frac{3}{5}$
(c) $\frac{1}{5}$
(d) $\frac{4}{5}$

| $1 .(d)$ | $2 .(a)$ | $3 .(b)$ | $4 .(c)$ | $5 .(d)$ | $6 .(b)$ | $7 .(6)$ | $8 .(c)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $9 .(c)$ | $10 .(d)$ | $11 .(6)$ | $12 .(c)$ | $13 .(d)$ | $14 .(d)$ | $15 .(6)$ |  |

II. Multiple choice questions

1. The height of a rectangle in a histogram shows the
[NCERI Exemplar]
a. width of the class
2. upper limit of the class
c. Lower limit of the class
d. frequency of the class
3. Listed below are the temperature in ${ }^{\circ} \mathrm{C}$ for 10 days.
[ $N(C E R T$ Exemplar]
$-6,-8,0,3,2,0,1,5,4,4$
What is the range of the data?
a. $\mathcal{S}^{0}$
4. $13{ }^{\circ} \mathrm{C}$
c. $10^{\circ} \mathrm{C}$ d. $12{ }^{\circ} \mathrm{C}$
5. A graph showing two sets of data simultaneously is known as
[NCERT Exe mplar]
a. pictograph
6. Gistogram
c. pie chart
d. double bar graph
7. Data represented using circles is Known as
a. 6ar graph
8. Kistogram
c. pictograph
d. pie chart
9. Data collected in a survey shows that $40 \%$ of the buyers are interested in buying a particular Grand of toothpaste. The centralangel of sector of the pie chart representing this information is
[NCERT Exemplar]
a. $120^{\circ}$
10. $150^{0}$
c. $144^{0}$
d. $40^{\circ}$
11. What is the probability of choosing a vowelfrom the alphabets?
[NCERT Exemplar]
a. $\frac{21}{26}$
12. $\frac{5}{26}$
c. $\frac{1}{26}$
d. $\frac{3}{26}$
[NCERI Exemplar]
a. Tossing a coin
13. Rolling a dice
c. Choosing a card from a deck of 52 cards
d. Throwing a stone from a roof of a building
14. Ram put some buttons on the table. There were 4 blue, 7 red, 3 black and 6 white buttons in all. All of a sudden, a cat jumped on the table and knocked out one button on the floor. What is the probability that the button on the floor is blue?
[EXERT Exemplar]
a. $\frac{7}{20}$
b. $\frac{3}{5}$
c. $\frac{1}{5}$
d. $\frac{1}{4}$
15. A coin is tossed 12 times and the outcomes are observed as shown below.


The chance of occurrence of $\mathcal{H e}$ ad is
$[\mathfrak{N C E R T}$ Exemplar]
a. $\frac{1}{2}$
6. $\frac{5}{12}$
c. $\frac{7}{12}$
d. $\frac{5}{7}$
10. $\mathcal{A}$ dice is tossed two times. The number of possible outcomes in $\qquad$ $[\mathcal{N C E R T}$ Exemplar]
a. 12
6. 24
c. 36
d. 30
11. A glass jar contains 6 red, 5 green, 4 blue and 5 yellow marbles of same size. Haritakes out a marble from the jar at random. What is the probability that the chosen marble is of red colour?
[ $N$ CEERT Exemplar]
a. $\frac{7}{10}$
6. $\frac{3}{10}$
c. $\frac{4}{5}$
d. $\frac{2}{5}$
12. Total number of outcomes, when a ball is drawn from a bag which contains 3 red, 5 black and 4 6lue balls is
[ $N$ CERT Exemplar]
a. 8
6.7
c. 9
d. 12
13. Number 1 to 5 are written on separate slips, i.e., one number on one slip and put in a box. Wahida pick a slip from the box without looking at it. What is the probability that the slip bears an odd number? [ $\mathcal{N C E R T}$ Exemplar]
a. $\frac{1}{5}$
6. $\frac{2}{5}$
c. $\frac{3}{5}$
d. $\frac{4}{5}$
14. A coin is tossed three times. The number of possible outcomes is
[ $N$ (CERT Exemplar]
a. 3
6. 4
c. 6
d. 8

| $1 . d$ | 2.6 | $3 . d$ | $4 . d$ | $5 . c$ | 6.6 | $7 . d$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $8 . c$ | 9.6 | $10 . c$ | 11.6 | $12 . d$ | $13 . c$ | $14 . d$ |

I. Fill in the blanks

1. Data available in an unorganise d form is called $\qquad$ data. [NCERT Exemplar]
2. In the class interval 20-30, the lower class limit is $\qquad$ - [ $N$ (CERT Exemplar]
3. In the class interval 26-33,33 is known as $\qquad$ - [NCERI Exemplar]
4. The range of the data $6,8,16,22,8,20,7,25$, is $\qquad$ - [ $\operatorname{NCERT}$ Exemplar]
5. A pie chart is used to compare $\qquad$ to a whole. [ $\mathcal{N C E R T}$ Exe mplar]

| 1. raw | 2.20 | 3. upper Cimit | 4.19 | 5.parts |
| :---: | :---: | :---: | :---: | :---: |

I. True or False

1. In a pie cfiart a whole circle is divided into sectors.[ $\mathcal{N C E R T}$ Exemplar]
2. The central angle of a sector in a pie chart cannot be more than $180^{\circ}$. [ $\mathcal{N C E E R}$ Exemplar]
3. Sum of all the central angles in a pie chart is $360^{\circ}$. [ $\mathcal{N C E R T}$ Exemplar]
4. In a pie chart two central angles can be of $180^{\circ}$. [ $\mathcal{N C E R T}$ Exemplar]
5. In a pie chart two or more central angles can be equal. [NCERT Examplar]

| 1. True | 2.False | 3. True | 4. True | 5. True |
| :---: | :---: | :---: | :---: | :---: |

I. Very Short Answer $\mathcal{T} y p e$ Questions.

1. Read the frequency distribution table given below answer the questions that follow:
[ $N$ (CERT Exemplar]

| Class Interval | Frequency |
| :---: | :---: |
| $25 \cdot 35$ | 1 |
| $35 \cdot 45$ | 5 |
| $45 \cdot 55$ | 5 |
| $55 \cdot 65$ | 4 |
| $65 \cdot 75$ | 8 |
| $75 \cdot 85$ | 25 |
| Total | 85 |

(a) Class interval which has the lowest frequency.
(6) Class interval which has the fighest frequency.
(c) What is the class size of the intervals?
(d) What is the upper limit of the fifth class?
(e) What is the lower limit of the last class?

Sol. (a) 65-75
(6) $75 \cdot 85$
(c) 10
(d) 75
(e) 85

## ()) Cext <br> Seneration

2. Given below is a frequency distribution table. Read it and answer the questions that follow.

| Class interval | Frequency |  |
| :--- | :--- | :--- |
| $10-20$ | 5 | 10 |
| $20-30$ | 4 | 15 |
| $40-40$ | 12 |  |
| $50-60$ |  |  |

(a) What is the lower limit of the second class interval?
(6) What is the upper limit of the last class interval?
(c) What is the frequency of the third class?
(d) Which interval frs a frequency of 10 ?
(e) Which interval has the lowest frequency?
(f) What is the class size? [ $\mathcal{N C E R I}$ Exemplar]

Sol. (a) 20
(b) 60
(c) 4
(d) 20-30
(e) 30-40
(f) 10
3. Classify the following statements under, -SPpropriate headings. [ $\mathcal{N C E R T}$ Exemplar]
(a) Getting the sum of angles of a triangle as $180^{\circ}$.
(6) India winning a cricket matcfagainst Pakistan.
(c) Sun setting in the evening.
(d) Getting 7 when a die is thrown.
(e) Sun rising from the west.
(f) Winning a racing competition by you.

| Certain to happen | Impossible to happen | May or may not happen |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |

Sol. (a) Certain to fappen
(6) May or may not fiapen
(c) Certain to fappen
(d) Impossible to happen
(e) Impossible to frappen
(f) May or may not happen
4. Look at the Gistogram below and answer the questions that follow. [NCERT Exemplar]

(a) How many students have fieight more than or equal to 135 cm but less than 150 cm ?
(6) Which class intervalhas the least number of students?
(c) What is the class size ?
(d) How many students have feight less than 140 cm ?

Sol. (a) $14+18+10=42$
(b) 150-155
(c) 5
(d) $6+8+14=28$


1. If we change the position of any of the bars of a graph, would it change the information being conveyed? Why?

If the height of a Gar remains unchanged, then changing of its position does not change the information being conveyed.
2. The following pie charts gives you a different piece of information about your class. Find the fraction of the circle representing the information.

3. Answer the following questions based on the pie chart given.
(i) Which type of programmes are viewed the most?
(ii) Which two types of programmes have number of viewers equal to those watching sports channels?


Viewers watching different types of channels on T.V.

Sol. (i) The entertainment programmes are viewed the most.
(ii) The news and informative programmes have the equal number of viewers to those watching sports channe ls.
4. Which form of graph would be appropriate to display the following data? Production of food gains of a state is given below.

| Year | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Production (in lakf tons) | 60 | 50 | 70 | 55 | 80 | 85 |

A bar graph will be an appropriate representation of the above data.
5. Which form of graph would be appropriate to display the following data? Choice of food for a group of people is given below.

| Favourite food | North Indian | South Indian | Chinese | Others | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathcal{N} u m b e r$ of people | 30 | 40 | 25 | 25 | 120 |

$\mathcal{A}$ circle graph (or a pie chart).
6. Which form of graph is appropriate to display the following data? The daily income of a group of a factory workers is given below.

| Daily income (in' ') | $\mathcal{N}$ (umber of workers (in a factory) |
| :---: | :---: |
| $75-100$ | 45 |
| $100-125$ | 35 |
| $125-150$ | 55 |
| $150-175$ | 30 |
| $175-200$ | 1250 |
| $200-225$ | 480 |
| $225-250$ | Total |

$\mathcal{A}$ fistogram would be appropriate representation of the above data.
7. When a die is thrown, what are the possible outcomes?

The possible outcomes are $1,2,3,4,5$ or 6 .
8. You have a bag with five identical balls of different colours (White, red, blue, green and yellow) and you are to pull out a ball without looking at it. List the outcomes you would get.

The possigle outcomes are $\mathcal{W}, \mathcal{R}, \mathcal{B}, \mathcal{G}$ or $\mathcal{Y}$.
9. When you spin the wheel shown, what are the possible outcomes?

The possifle outcomes are $\mathcal{A}, \mathcal{B}$ or $\mathcal{C}$.


1. Given below are the height (in cm) of 11 boys of a class:
$146,143,148,132,128,139,140,152,154,142,149$ Arrange the above data in ascending order and find :
(a) the height of the tallest boy.
(6) the height of the shortest boy.
(c) the range of the given data. [NCERT Exemplar]

Sol. Arranging the given data in ascending order, we get the feight (in cm) as :
$128^{\prime} 132,139,140,142,143,146,148,149,152,154$.
(a) 154
(6) 128
(c) 26
2. The following pie chart depicts the expenditure of a state government under different heads.
(a) If the total spending is 10 crores, how much money was spent on roads ?
(6) How many times is the amount of money spent on education compared to the amount spent on roads ?
(c) What fraction of the total expenditure is spent on both roads and public welfare together?


Sol. (a) Money spent on roads $=10 \%$ of 10 crores
(9) $=\frac{10}{100}$ x 10 crores $=1$ crore
(6) Money spent on education $=25 \%$ of 10 crores

$$
=25000000
$$

Money spent on road $=10000000$
$\Rightarrow \quad \frac{25000000}{10000000}-2.5$ times
(c) Totalexpenditure $=100000000$

Money spent on both roads and public welfare

$$
=10 \%+20 \%=30 \%
$$

So, fraction $=\frac{3 \text { crores }}{10 \text { crores }}=\frac{3}{10}$
3. Following are the number of members in 25 families of a village $6,8,7,7,6,5,3,2$, $5,6,8,7,7,4,3,6,6,6,7,5,4,3,3,2,5$. Prepare a frequency distribution table for the data using class intervals $0-2,2-4$, etc.
[NCERT Exemplar] Sol.

| Class interval | Tally marks | Frequency |
| :---: | :---: | :---: |
| $0-2$ |  | 0 |
| $2-4$ | NN । | 6 |
| $4-6$ | NV । | 6 |
| $6-8$ | NN NN । | 11 |
| $8-10$ | I\| | 2 |
|  | Total | 25 |

4. The marks obtained (out of 20) by 30 students of a class in a test are as follows:
[ $\mathcal{N C E R T}$ Exemplar]
$14,16,15,11,15,14,13,16,8,10,7,11,18,15,14,19,20,7,10,13,12$,
$14,15,13,16,17,14$,
11, 10, 20. Prepare a frequency distribution table for the above data using class intervals of equal width one class interval is $4-8$ (excluding 8 and including 4.) Sol.

| Class interval | Tally marks | Frequency |
| :---: | :---: | :---: |
| $4-8$ | $\\|$ | 2 |
| $8-12$ | NN \\| \| | 7 |
| $12-16$ | NN \\| II | 13 |
| $16-20$ | IN | 6 |
| $20-24$ | Total | 30 |

5. Draw a fistogram to represent the frequency distribution for the number of members in 25 families of a village $6,8,7,7,6,5,3,2,5,6,8,7,7,4,3,6,6,6,7,5,4$, $3,3,2,5$.

Sol.

6. Ritwik draws a ball from a bag that contains white and yellow balls. The probability of choosing a white ball is $\frac{\mathbf{2}}{\mathbf{9}}$. If the total number of balls in the 9 bag is 36 , find the number of yellow balls.

Sol. Let no. of yellow ball, in a bag $=x$
Then, probability of choosing yellow ball

$$
=P(Y)=\frac{x}{36}
$$

and probability of choosing white ball

$$
\begin{array}{cc} 
& P(W)=\frac{2}{9}(\text { give } n) \\
\therefore & P(Y)+P(W)=1 \\
& \frac{x}{36}+\frac{2}{9}=1 \\
& \frac{x+8}{36}=1 \Rightarrow x+8=36 \\
\Rightarrow & x=28
\end{array}
$$

$$
\therefore \quad \mathcal{N} \text { o. of yellow balls }=28
$$

7. Given below is a pie chart showing the time spend by a group of 350 cfildren in different games. Observe it and answer the questions that follow.
(a) How many cfildren spend at least less than one four in playing games ?
(6) How many children spend more than 2 fours in playing games ?
(c) How many cfildren spend 3 or lesser fours in playing games ?
(d) Which is greater - number of children who spend 2 hours or more per day or number of children who play for less than one hour? [NCERI Exemplar]

Sol. (a) Less than 1 four $=6 \%$ of $350=\frac{6 \times 350}{100} 21$
$\therefore \mathcal{N}$ o.of Children who spend at least less than one frour $=350-21=329$
(6) More than 2 fours $=34 \%+10 \%+4 \%=48 \%$

$$
\frac{48 \times 350}{100}=168
$$

(c) 3 or lesser hours $=6 \%+16 \%+30 \%+34 \%=86 \%$

$$
\frac{86 \times 350}{100}=301
$$

(d) 2 four or more is greater number
8. In a survey of 200 ladies, it fas found that 82 like coffee while 118 dislike it. From these ladies, one is chosen at random. What is the probability that the chosen lady dislikes coffee ?

Sol. Since, Total number of outcomes $=200$
and

$$
\text { Like coffee }=82
$$

and

$$
\text { Dislike coffee }=118
$$

We know that,
Probability of an event $\mathcal{P}(\mathcal{E})$

$$
=\frac{\text { Favourable Outocmes }}{\text { Total number of outcomes }}
$$

Then, $\mathcal{P}($ dislike coffee $)=\frac{118}{200}=\frac{59}{100}$
II. Sfort Answer Type Questions.

1. The top speed of thirty different land animals have been organised into a frequency table. Draw a fistogram for the given data. [NCERT Exemplar]

2. Classify the following statement under appropriate headings.
(i) Getting the sum of angles of a triangle as $180^{\circ}$.
(ii) India winning a cricket match against Pakistan.
(iii) Sun setting in the evening.
(iv) Getting 7 when a die is thrown.
(v) Sun rising from the West.
(vi) Winning a racing competition by you.

Sol.

| Certain to Kappen | Impossible to happen | May or may not happen |
| :---: | :---: | :---: |
| (i) | (iv) | (ii) |
| (iii) | (v) | (vi) |

3. Ritwik draws a ball from a bag that contains white and yellow balls. The probability 92 of choosing a white ball is - If the total number of balls in the bag is 36, find the number of yellow balls.
[NCERI Exemplar]
Sol. Total number of outcomes $=36$
$\mathcal{P}($ Choosing a white 6 all $)=\frac{\text { Number of white balls }}{\text { Total number of balls }}$

$$
\frac{2}{9}=\frac{\text { Number of white balls }}{36}
$$

$\mathcal{N}$ umber of white balls $=\frac{2 \times 36}{9}=8$
The number of yellow balls $=36-8=28$
4. Look at the histogram below and answer the questions that follow. [ $\mathcal{N C E R T}$ Exemplar]

(i) How many students have height more than or equal to 135 cm but less than 150 cm ?
(ii) Which class interval has the least number of students?
(iii) What is the class size?
(iv) How many students have height less than 140 cm ?

Sol. (i) Number of students faving height more than or equal to 135 cm but less than $150 \mathrm{~cm}=14+18+10=42$.
(ii) 150-155 have Le ast number of students.
(iii) Class size $=$ upper class limit-Lower class limit $=155-150=5$.
(iv) $\mathcal{N}$ umber of student having height less than $140 \mathrm{~cm}=6+8+14=28$.
5. Following are the number of members in 25 families of a village: 6, 8, 7, 7, 6, 5, 3, 2, $5,6,8,7,7,4,3,6,6,6,7,5,4,3,3,2,5$. Prepare a frequency distribution table for the data using class intervals [NCERT Exemplar] Sol.

| Class Interval | Tally marks | Frequency |
| :---: | :---: | :---: |
| $0-2$ |  | 0 |
| $2-4$ | $N N \mid$ | 6 |
| $4-6$ | $M N\|N\|$ | 6 |
| $6-8$ | $\\|$ | 11 |
| $8-10$ | Total | 2 |
|  |  | $\mathbf{2 5}$ |

6. Draw a fistogram to represent the frequency distribution as per the table given in question 5. [NCERT Exemplar] Sol.

7. The marks obtained (out of 20) by 30 students of a class in a test are as follows:
$14,16,15,11,15,14,13,16,8,10,7,11,18,15,14,19,20,7,10,13,12$, $14,15,13,16,17,14,11,10,20$.

Prepare a frequency distribution table for the above data using class intervals of equal width in which one class interval is $4-8$ (excluding 8 and including 4).
[ $N$ CERT Exemplar]

| Class Interval | Tally marks | Frequency |
| :---: | :---: | :---: |
| $4-8$ | $\\|$ | 2 |
| $8-12$ | $\ N \\|$ | 7 |
| $12-16$ | $N N\\|\\|$ | 13 |
| $16-20$ | $N N \\|$ | 6 |
| $20-24$ | $\\|$ | 2 |
|  | Total | 30 |

8. Prepare a fistogram from the frequency distribution table obtained in questions?

9. The weight (in kg ) of 30 students of a class are: 39, 38, 36, 38, 40, 42, 43, 44, 33, $33,31,45,46,38,37,31,30,39,41,41,46,36,35,34,39,43,32,37,29,26$. Prepare a frequency distribution table using one class interval as (30-35), 35 not included.
[ $\mathcal{N C E R T}$ Exe mplar]
(i) Which class fas the least frequency?
(ii) Which class has the maximum frequency?

Sol.

| Class Interval | Tally marks | Frequency |
| :---: | :---: | :---: |
| $25-30$ | $\\|\\|\\|\\|$ | 2 |
| $30-35$ | $\wedge N\\|\\|$ | 7 |
| $35-40$ | $\lfloor N \\|$ | 11 |
| $40-45$ | $\\|\\|$ | 7 |
| $45-50$ | Total | 3 |
|  |  | 30 |

10. Construct a frequency distribution table for the following weights (in grams) of 35 mangoes, using the equal class intervals, one of them is 40-45 (45 not included). $30,40,45,32,43,50,55,62,70,70,61,62,53,52,50,42,35,37,53,55$, $65,70,73,74,45,46,58,59,60,62,74,34,35,70,68$.
(i) How many classes are there in the frequency distribution table?
(ii) Which weight group has the highest frequency? [ $\mathcal{N C E R T}$ Exemplar]

Sol.

| Class Interval | Tally marks | Frequency |
| :---: | :---: | :---: |
| $30-35$ | $\\|\\|$ | 3 |
| $35-40$ | $\\|\\|$ | 3 |
| $40-45$ | $\\|\\|$ | 3 |
| $45-50$ | $\\|\\|$ | 3 |
| $50-55$ | $\\| N$ | 5 |
| $55-60$ | $\\| N$ | 4 |
| $60-65$ | $\\|$ | 5 |
| $65-70$ | $N\\|\\|$ | 2 |
| $70-75$ | Total | 7 |
|  |  | 35 |

(i) 9
(ii) 70-75
11. Draw a histogram for the following data.
[NCERI Exemplar]

| Class Interval | $10-15$ | $15-20$ | $20-25$ | $25-30$ | $30-35$ | $35-40$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 30 | 98 | 80 | 58 | 29 | 50 |

Sol.

12. The below fistogram shows the number of literate femates in the age group of 10 to 40 years in a town.

(i) Write the classes assuming all the classes are of equal width.
(ii) What is the class width?
(iii) In which age group are literate females the least?
(iv) In which age group is the number of literate females the highest? [NCERT Exemplar]

Sol.
(i) $10-15,15-20,20-25,25-30,30-35,35-40$ are the classes of equal width.
(ii) 5 is the class width.
(iii) $10-15$ is the age group in which literate females are the le ast.
(iv) $15-20$ is the age group in which literate females are the fighest.
13. Draw an appropriate graph to represent the given information.

| Month | Iul. | Aug. | Sept. | Oct. | $\mathcal{N}$ Nov. | $\mathcal{D e c}$. |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of watches sold | 1000 | 1500 | 1500 | 2000 | 2500 | 1500 |


14. Percentage wins in $O D$ ! $6 y 8$ top cricket teams.

| Teams | From champions trophy <br> to world Cup-06 | Last 10 ODI in 07 |
| :---: | :---: | :---: |
| South Africa | $75 \%$ | $78 \%$ |
| Australia | $61 \%$ | $40 \%$ |
| Sri Lanka | $54 \%$ | $38 \%$ |
| New Zealand | $47 \%$ | $50 \%$ |
| England | $46 \%$ | $50 \%$ |
| Pakistan | $45 \%$ | $44 \%$ |
| West Indies | $44 \%$ | $30 \%$ |
| India | $43 \%$ | $56 \%$ |

Draw a double bar graph for the above date.
Sol. Note: $\mathcal{A}$ bar grapf showing two sets of data simultaneously is called a double-bar graph. It is usefulfor the comparison of the data.

I. Long Answer Type Questions.

1. The number of cycles produced in a factory during five consecutive weeks is given below:

| Week | First | Second | Third | Fourth | Fifth |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathcal{N}$ umber of cycles produced | 800 | 1300 | 1060 | 920 | 1440 |

Draw a bar graph representing the above information.
Sol. We candraw the bar graph by using the following steps:
Step 1. On a grapf paper, draw a forizontalline $O X$ and a verticalline $O \mathcal{Y}$, representing the $x$-axis and $y$-axis respectively.

Step 2. Along OX, mark the weeks at points taken at equalgaps.
Step 3. Choose the scale:
1 small division $=20$ cycles
Step 4. The height of the bars are: $1 \times 800,20$
Production in the 1st we ak $=\left(\frac{1}{20} \times 800\right)$

$$
=40 \mathrm{small} \text { divisions }
$$

Production in the $2^{\text {nd }}$ we ak $=\left(\frac{1}{20} \times 1300=65\right.$
small divisions.
Production in the $3^{\text {rd }}$ we $a k=\left(\frac{1}{20} \times 1300=53\right.$ small divisions.
Production in the $4^{\text {th }}$ weak $=\left(\frac{1}{20} \times 920=46 \mathrm{small}\right)$ divisions.
Production in the $5^{\text {th }}$ weak $=\left(\frac{1}{20} \times 1440\right)=72$ small divisions.
Step 5. Draw bars of equal width and heights calculated in step 4 at the points marked in step 2.

The bar graph is shown below:

2. Shoes of the following brands are sold in $\mathcal{N}$ (ov. 4:107 at a shoe store. Construct a pie chart for the data.
[ $N$ CERT Exe mplar]

| $\mathcal{B r a n d}$ | $\mathcal{N}$ umber of pair of shoes sold |
| :---: | :---: |
| $\mathcal{A}$ | 130 |
| $\mathcal{B}$ | 120 |
| $\mathcal{C}$ | 90 |
| $\mathcal{D}$ | 40 |
| $\mathcal{E}$ | 20 |

Sol. Totalnumber of shoes $=400$
We find the central angle for each sector

| Brand | Number of <br> shoes | In fraction | central angle |
| :---: | :---: | :---: | :---: |
| A | 130 | $\frac{130}{400}=\frac{13}{40}$ | $\frac{13}{40} \times 360^{\circ}=117^{\circ}$ |
| B | 120 | $\frac{120}{400}=\frac{3}{10}$ | $\frac{3}{10} \times 360^{\circ}=108^{\circ}$ |
| C | 90 | $\frac{90}{400}=\frac{9}{40}$ | $\frac{9}{40} \times 360^{\circ}=81^{\circ}$ |
| D | 40 | $\frac{40}{400}=\frac{1}{10}$ | $\frac{1}{10} \times 360^{\circ}=36^{\circ}$ |
| E | 20 | $\frac{20}{400}=\frac{1}{20}$ | $\frac{1}{20} \times 360^{\circ}=18^{\circ}$ |

The pie chart is

3. Draw a pie chart for the given data.

| Favourite food | Number of pe ople |  |
| :--- | :--- | :--- |
| North Indian | 30 |  |
| South Indian | 40 |  |
| Chinese | 25 |  |
| Others | 25 |  |

Sol. Total number of people $=120$
We find the central angle for each sector.

| Favourite <br> food | Number <br> of people | In <br> fraction | Central angle |
| :---: | :---: | :---: | :---: |
| North Indian | 30 | $\frac{30}{120}=\frac{1}{4}$ | $\frac{1}{4} \times 360^{\circ}=90^{\circ}$ |
| South Indian | 40 | $\frac{40}{120}=\frac{1}{3}$ | $\frac{1}{3} \times 360^{\circ}=120^{\circ}$ |
| Chinese | 25 | $\frac{25}{120}=\frac{5}{24}$ | $\frac{5}{24} \times 360^{\circ}=75^{\circ}$ |
| Others | 25 | $\frac{25}{120}=\frac{5}{24}$ | $\frac{5}{24} \times 360^{\circ}=75^{\circ}$ |

The pie chart is

4. A dice in rolled once. What is the probability that the number on top will be
[ $\mathcal{N C E R T}$ Exemplar]
(a) $O d d$
(6) Greater than 5
(c) A multiple of 3
(d) Less than 1
(e) $\mathcal{A}$ factor of 36
(f) A factor of 6

Sol. (a) Totalno. in a dice $=6$

$$
O d d=1,3,5 \text { i.e. } 3 \text { numbers }
$$

$\therefore \quad$ Probability $=\frac{3}{6}=\frac{1}{2}$
(6) Greater than $5=6$ i.e. 1 number
$\therefore \quad$ Probability $=\frac{1}{6}$
(c) Multiple of $3=3,6$ i.e. 2 numbers

Probability $=\frac{2}{6}=\frac{1}{3}$
(d) Less than $1=$ no number i.e. 0

$$
\text { Probability }=\frac{0}{6}=0
$$

(e) Factor of $36=1,2,3,4,6$ i.e. 5 numbers

Probability $=\frac{5}{6}$
(f) Factor of $6=1,2,3,6$ i.e. 4 numbers

Probability $=\frac{4}{6}=\frac{2}{3}$
5. In a hypothetical sample of 20 people, the amount of money (in thousands of rupees) with each was found to be as follows:
$114,108,100,98,101,109,117,119,126,131,136,143,156,169,182,195,207,219$,
235,118 .
Draw a kistogram of the frequency distribution, taking one of the class interval as 50-100.
[NCERI Exemplar]

| Class Interval | Frequency |
| :---: | :---: |
| $50-100$ | 1 |
| $100-150$ | 12 |
| $150-200$ | 4 |
| $200-250$ | 3 |


II. Long Answer Type Questions.

1. Given below is a frequency distribution table. Read it and answer the questions that follow:

| Class Interval | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 5 | 10 | 4 | 15 | 12 |

i. What is the lower limit of the second class interval?
[ $N$ CERT Exemplar]
ii. What is the upper limit of the last class interval?
iii. What is the frequency of the third class?
iv. Which interval has a frequency of 10 ?
v. Which interval has the lowest frequency?
vi. What is the class size?

Sol. i. The second class interval is 20-30.

$$
\therefore \quad \text { The lower limit }=20
$$

ii. The last class interval $=50-60$
iii. The upper limit $=60$ The frequency of the third class (30-40) $=4$
iv. The class interval having frequency $10=20-30$
v. The interval having lowest frequency $=30-40$
vi. The class size = upperclass limit-lowerclass limit $=20-10=10$
2. Given below is a pie chart showing the time spend by a group of 350 children in different games. Observe it and answer the questions that follow. [ $\mathcal{N C E R T}$ Exemplar]
(i) How many children spend at le ast one four in playing games?
(ii) How many children spend more than 2 hours in playing games?
(iii) How many children spend 3 or lesser hours in playing games?
(iv) Which is greater - number of children who spend 2 fours
 or more per day or number of children who play for less than one fiour?

Sol. (i) Totalpercentage of children who spend at least one four in playing games

$$
=16 \%+30 \%+34 \%+10 \%+4 \%=94 \% .
$$

$\mathcal{N u m b e r}$ of children who spend at least one hour in playing games

$$
=94 \% \text { of } 350=\frac{94}{100} \times 350=329
$$

(ii) Total percentage of cfildren who spend more than 2 fours in playing games

$$
=34 \%+10 \%+4 \%=48 \%
$$

$\mathcal{N}$ umber of children who spend more than 2 fours in playing games

$$
=48 \% \text { of } 350=\frac{48}{100} \times 350=168
$$

(iii) Total percentage of children who spend 3 or less hours in playing games

$$
=34 \%+30 \%+16 \%+6 \%=86 \%
$$

$\mathcal{N}$ umber of children who spend 3 or less hours in playing games

$$
=86 \% \text { of } 350=\frac{86}{100} \times 350=301
$$

(iv) Total percentage of children who spend 2 hours or more per day

$$
=30 \%+34 \%+10 \%+4 \%=78 \%
$$

$\mathcal{N}$ umber of cfildren who play 2 fours or more per day

$$
=78 \% \text { of } 350=\frac{78}{100} \times 350=273
$$

$\mathcal{N}$ umber of children who play for less than one four

$$
=6 \% \text { of } 350=\frac{6}{100} \times 350=21
$$

Therefore, number of children who play for 2 fours or more per day is greater.
3. The pie chart below shows the result of a survey carried out to find the modes of travel used by the children to go to school. Study the pie chart and answer the questions that follow.
[ $N(C E R I$ Exe mplar]
(i) What is the most common mode of transport?
(ii) What fraction of children travel by car?
(iii) If 18 children travel by car, how many children took part in the survey?
(iv) How many children use taxi to travel to school?
(v) By which two modes of transport are equal number of children travelfing?


Sol. (i) The most common mode of transport is Bus. $90^{\circ}$
(ii) Fraction of children travel bycar $=360^{\circ}=4$
(iii) $90^{\circ}$ represent 18 children $18360^{\circ}$ represents $=90 \times 360=72$ Hence, number of children who took part in the survey are 72
(iv) Central angle for taxi $=360^{\circ}-\left(60^{\circ}+120^{\circ}+90^{\circ}+60^{\circ}\right)=360^{\circ}-330^{\circ}=30^{\circ} 30$
$\mathcal{N}$ (umber of children who use taxi $=360 \times 72=6$
(v) Cycle and walk are the mode that equal number of children are using.
4. A dice is rolled once. What is the probability that the number on top will be
(i) $O d d$
(ii) Greater than 5
(iii) $\mathcal{A}$ multiple of 3
(iv) Less than 1
(v) A factor of 36
(vi) A factor of 6

Sol. On rolling a die, all possible outcomes are 1, 2, 3, 4, 5, 6
Total number of possible outcomes $=6$
(i) Odd number on the top of a die $=1,3,5$

Number of favourable outcomes $=3$

$$
\begin{aligned}
P(\text { getting odd number on the top })= & \frac{\text { Number of favourable outcomes }}{\text { Total number of outcomes }} \\
& =\frac{3}{6}-\frac{1}{2}
\end{aligned}
$$

(ii) $\mathfrak{N u m b e r}$ of favourable outcome $=1$ ( 6 only)
$\therefore \quad$ Required probability $=\frac{1}{6}$
(iii) Number of favourable outcomes $=2$ i.e, 3 and 6

Required probability $\frac{2}{6}=\frac{1}{3}$
(iv) Number of favourable outcome $=0$
$\therefore \quad \operatorname{P}($ getting number less than 1$)=\frac{0}{6}=0$
(v) $\mathcal{N}$ umber on top that are factor of $36=1,2,3,4,6$
$\mathcal{N}$ umber of favourable outcomes $=\frac{5}{6}$

$$
\mathcal{P}(\text { a factor of } 36)=\frac{4}{6} \text { or } \frac{2}{3}
$$

(vi) $\mathcal{A}$ factor of $6=1,2,3,6$
$\mathcal{N}$ umber of favourable outcomes $=4$
$\mathcal{P}($ a factor of 6$)=\frac{4}{6}$ or $\frac{2}{3}$.
5. Shoes of the following brands are sold in $\mathcal{N}$ (ov. 2007 at a shoe store. Construct a Pie chart for the data.

## [ $N(C E R T$ Exe mplar]

| $\mathcal{B r a n d}$ | $\mathcal{A}$ | $\mathcal{B}$ | $\mathcal{C}$ | $\mathcal{D}$ | $\mathcal{E}$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathcal{N u m b e r}$ of pair of shoes sold | 130 | 120 | 90 | 40 | 20 |
|  |  |  |  |  |  |

Sol. We know that central angle for a sector $=\frac{\text { Value of the component }}{\text { Total Value }} \times 360^{\circ}$
Here total number of pair of shoes $=400$
Central angle for a 6 rand $=\frac{\text { Number of shoes sold in brand }}{\text { Total Number of shoes sold }} \times 360^{\circ}$
Calculation of central angles:

| Brand | Number of pair of <br> shoes sold | In Fractions | Central angle |
| :---: | :---: | :---: | :---: |
| A | 130 | $\frac{130}{400}=\frac{13}{40}$ | $\frac{13}{40} \times 360^{\circ}=117$ |
| B | 120 | $\frac{120}{400}=\frac{3}{10}$ | $\frac{3}{10} \times 360^{\circ}=108^{\circ}$ |
| C | 90 | $\frac{90}{400}=\frac{9}{40}$ | $\frac{9}{40} \times 360^{\circ}=81^{\circ}$ |
| D | 40 | $\frac{40}{400}=\frac{1}{10}$ | $\frac{1}{10} \times 360^{\circ}=36^{\circ}$ |
| E | 20 | $\frac{1}{400}$ | $\frac{1}{20} \times 360^{\circ}=18^{\circ}$ |

Construction of pie chart

Steps of Construction
(i) $\operatorname{Draw}$ a circle with any convenient radius.
(ii) The angle of the sector for $\mathcal{A}$ is $117^{\circ}$.
(iii) Continue drawing the remaining centralangles.
(iv) Shade the sectors so obtained with different design and labeleach of them.

6. For the development of basic infrastructure in a district, a project of Z108 crore approved by Development $\mathcal{B a n k}$ is as follows:

| Item Head | Road | Electricity | Drinking water | Sewerage |
| :---: | :---: | :---: | :---: | :---: |
| Amount in crore () | 43.2 | 16.2 | 27.00 | 21.6 |

Draw a pie chart for this data.
Sol. Central angle for an ite $m=\frac{\text { Amount approved for an item }}{\text { Total amount }} \times 360^{0}$
Calculation of pie chart

| Items | Amount in crore (₹) | In Fractions | Central angle |
| :--- | :---: | :---: | :---: |
| Road | 43.2 | $\frac{43.2}{108}=\frac{2}{5}$ | $\frac{2}{5} \times 360^{\circ}=144^{\circ}$ |
| Electricity | 16.2 | $\frac{16.2}{108}=\frac{3}{20}$ | $\frac{3}{20} \times 360^{\circ}=54^{\circ}$ |
| Drinking water | 27.00 | $\frac{27}{108}=\frac{1}{4}$ | $\frac{1}{4} \times 360^{\circ}=90^{\circ}$ |
| Sewerage | 21.6 | $\frac{21.6}{108}=\frac{1}{5}$ | $\frac{1}{5} \times 360^{\circ}=72^{\circ}$ |



7. The following data represents the approximate percentage of water in various oceans. Prepare a pie chart for the given data.

| Pacific | $40 \%$ |
| :--- | :--- |
| Atlantic | $30 \%$ |
| Indian | $20 \%$ |
| Others | $10 \%$ |

Sol. Total angle at the centre of the circle is $360^{\circ}$, we make a table to find the central angle of the sectors.

| Oceans | Percentage of <br> water | In Fractions | Central angle |
| :---: | :---: | :---: | :---: |
| Pacific | $40 \%$ | $\frac{40}{100}=\frac{2}{5}$ | $\frac{2}{5} \times 360^{\circ}=144^{\circ}$ |
| Atlantic | $30 \%$ | $\frac{30}{100}=\frac{3}{10}$ | $\frac{3}{10} \times 360^{\circ}=108^{\circ}$ |
| Indian | $20 \%$ | $\frac{20}{100}=\frac{1}{5}$ | $\frac{1}{5} \times 360^{\circ}=72^{\circ}$ |
| Others | $10 \%$ | $\frac{10}{100}=\frac{1}{10}$ | $\frac{1}{10} \times 360^{\circ}=36^{\circ}$ |

The pie chart is drawn as follows:

8. Sonia picks up a card from the given cards.


Calculate the probability of getting
(i) an odd number
(ii) a $\mathcal{Y}$ card
(iii) a Gcard
(iv) $\mathcal{B}$ card bearing number $>7$

Sol. (i) Odd number in the given cards are 1,3,5,7 and 9
$\mathcal{N u m b e r}$ of favourable outcomes $=5$
Total number of outcomes $=10$
Probability of getting an odd number $=\frac{\text { Number of favourable outcomes }}{\text { Total number of outcomes }}$

$$
=\frac{5}{10}=\frac{1}{2}
$$

(ii) The $\mathcal{Y}$ cards are 2, 3, and 8
$\therefore \mathcal{N}$ umber of favourable outcomes $=3$
Total number of outcomes $=10$
$\mathcal{P}($ getting a $\mathcal{Y} \operatorname{card})=\frac{3}{10}$
(iii) The $\mathcal{G}$ cards are 7 and 10.
$\therefore \mathcal{N}$ umber of favourable outcomes $=2$
Total number of outcomes $=10$
$\mathcal{P}($ getting a $\mathcal{G} \operatorname{card})=\frac{2}{10}=\frac{1}{5}$
(iv) $\mathcal{B}$ card bearing number $>7$ is zero.
$\therefore$ Favourable number of outcomes $=0$
(2) $\mathcal{P}$ getting $\mathcal{B}$ card bearing number $>7)=\frac{0}{10}=0$
9. Observe the fistogram figure and answer the questions given below:

i. What information is being given by the histogram?
ii. Which group contains maximum girls?
iii. How many girls have a height of 145 cm and more?
iv. If we divide the girls into the following three categories, how many would there be in each?

$$
\begin{aligned}
& 150 \mathrm{~cm} \text { and more-Group } \mathcal{A} \\
& 140 \mathrm{~cm} \text { to less than } 150 \mathrm{~cm} \text { Group } \mathcal{B} \\
& \text { Less than } 140 \mathrm{cm-Group} \mathrm{C}
\end{aligned}
$$

Sol. i. The above histogram represents the height (in cm) of girls of Class VIII.
ii. The group 140-145 contains maximum number of girls (which has as much as 7 gir (s).
iii. 7 girls $(=4+2+1)$ fave a height of 145 cm and more.
iv. Number of girls in

Group $\mathcal{A}: 150 \mathrm{~cm}$ and more $=2+1=3$ gir $l_{s}$
Group $\mathcal{B}: 140 \mathrm{~cm}$ to lessthan $150 \mathrm{~cm}=7+4=11 \mathrm{girls}$
Group $C$ : Less than $140 \mathrm{~cm}=1+2+3=6$ girls
I. High Order Thinking Skills [HOTS] Questions.

1. It is known that a box of 100 electric bulbs contains 8 defective bulbs. One bulb is taken out at random from the box. What is the probability that the bulb drawn is :
[ $N$ (CERI Exemplar]
(a) defective
(6) non-defective. Sol. Since,

Total no. of outcomes $=100($ bulbs $)$
Totalno. of defective $\quad$ иulbs $=8$
Then, Total no. of non-defective bulbs=100-8=92
We know that,
$\therefore \quad$ Probability of an event, $\mathcal{P}(\mathcal{E})$

$$
=\frac{\text { Favourable outcomes }}{\text { Total number of outcomes }}
$$

Therefore,
(a) $\mathcal{P}\left(\right.$ defective $b u(G s)=\frac{8}{100}=\frac{2}{25}$
(b) $\mathcal{P}\left(\right.$ non-defective $6 u(b s)=\frac{92}{100}=\frac{23}{25}$
II. High Order Thinking Skills [ $\mathcal{H} O \mathcal{T S}]$ Questions.

1. The following pie chart depicts the expenditure of a state government under different heads.
i. If the total spending is 10 crores, howmuch money was spent on roads?
ii. How many times is the amount of money spent on education compared to the amount spent on roads? iii. What fraction of the total expenditure is spent on both roads and public welfare together?


Sol. i. Totalexpenditure $=10$ crores
Money spent on roads $=10 \%$ of 10 croroes

$$
=\frac{10}{100} \times 10 \text { crores }=1 \text { crore }
$$

ii. The amount of money spent on education $=25 \%$ of 10 crores

$$
=\frac{25}{100} \times 10=2.5 \text { crores }
$$

$$
\frac{\text { Money spent on education }}{M o n e y ~ s p e n t ~ o n ~ r o a d s ~}=\frac{2.5 \text { crores }}{1 \text { crore }}=2.5
$$

$\therefore$ Money spent on education is 2.5 times Money spent on roads.
iii. Total expenditure spend on roads and public welfare toge ther.

$$
=20 \%+10 \%
$$

Required fraction $=\frac{30}{100}=\frac{3}{10}$
2. Identify which symbol should appear in each section.


Sol. Total value $800+700+550+450=2500$
$32 \%$ represents $\frac{32}{100} \times 2500=800$
Therefore, $32 \%$ represents the symbol
$28 \%$ represents $\frac{28}{100} \times 2500=700$
Therefore $28 \%$ represents the symbol
$22 \%$ represent $\frac{22}{100} \times 2500=550$
Therefore $22 \%$ represents the symbol
$18 \%$ represents $\frac{18}{100} \times 2500=450$
Therefore $18 \%$ represents the symbol
I. Value Based Questions.

1. (a) In a lottery, there are 10 prizes and 20 6lanks. A ticket is chosen at random, what is the probability of getting a prize ?
(6) Study the following pictograph and answer the questions given below it.

|  |  | $40^{\text {ame }}$ | $=50$ cars |
| :---: | :---: | :---: | :---: |
| July | $\frac{0}{4}$ | $0^{2 m}$ |  |
| August | $0^{2}$ | $40^{2 \pi} 0$ |  |
| September | $40$ |  | $0^{2}$ |

(a) How many cars were produced in the month of $\mathcal{I} u l y$ ?
(6) In which month were maximum number of cars produced?

Sol. (a) Since, totalno. of outcomes $=10+20=30$
$\therefore \quad$ Probability of an event,
$P(E)=\frac{\text { Favourable outcomes }}{\text { Favourable outcomes }}$
Then, $\mathcal{P}($ getting a prize $)=\frac{10}{30}=\frac{1}{3}$
(a) 250 cars were produced in the month of $\mathcal{I} u l y$.
(6) Maximum number (= 400) of cars were produced in the month of September.


Eshool

